## Concentration of the posterior

## Doob's convergence



## Bernstein-von Mises Theorem (or Bayesian central-limit theorem): For a large n the *posterior* can be approximated by a normal distribution.

 $p(\boldsymbol{\theta}|\boldsymbol{y}) \approx \mathcal{N}(\hat{\boldsymbol{\theta}}, I(\hat{\boldsymbol{\theta}})^{-1})$ 

## Consequences:

- Bayesian methods and frequentist procedures based on maximum likelihood give, for large enough *n*, very close results
- the *posterior* can be computed as a normal whose mean and variance we can calculate simply using the MAP